

Better together: Simulation and Optimization work better together

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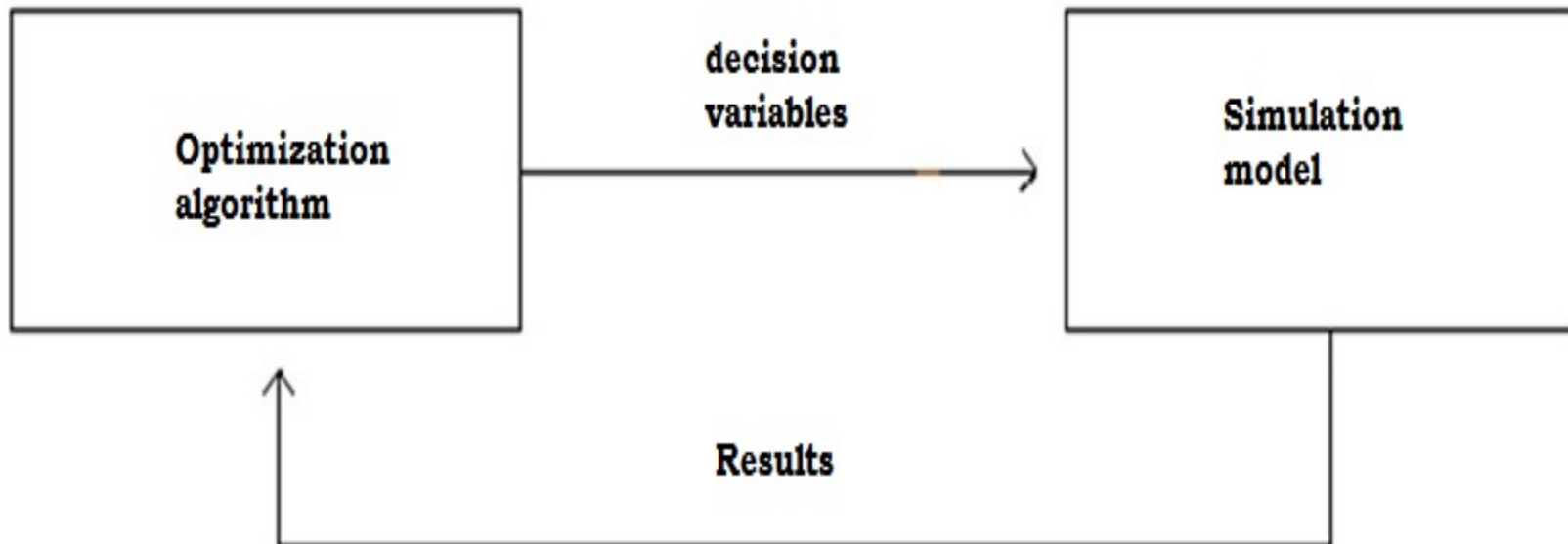
Introduction

- We present here a hybrid methodology that uses optimization and simulation techniques to analyze different cases in transport and to be able to find some that require optimal solutions

Objective

To design a flexible methodology to analyze, evaluate and optimize transport processes and services through the combined use of optimization and simulation techniques

Relationship simulation and optimization



Background

Since its inception, simulation teams have sought to optimize the problems they solve:

- 1995 Promodel includes SimRunner with evolutionary algorithms.
- 2004 Arena includes Optquest with scattered search algorithms.
- 2010 Simio includes OptQuest that uses metaheuristic procedures, including Tabu Search, Neural Networks, Scatter Search, and Linear/Integer Programming, into a single composite method.

Methodology

- Drawbacks if they work separately

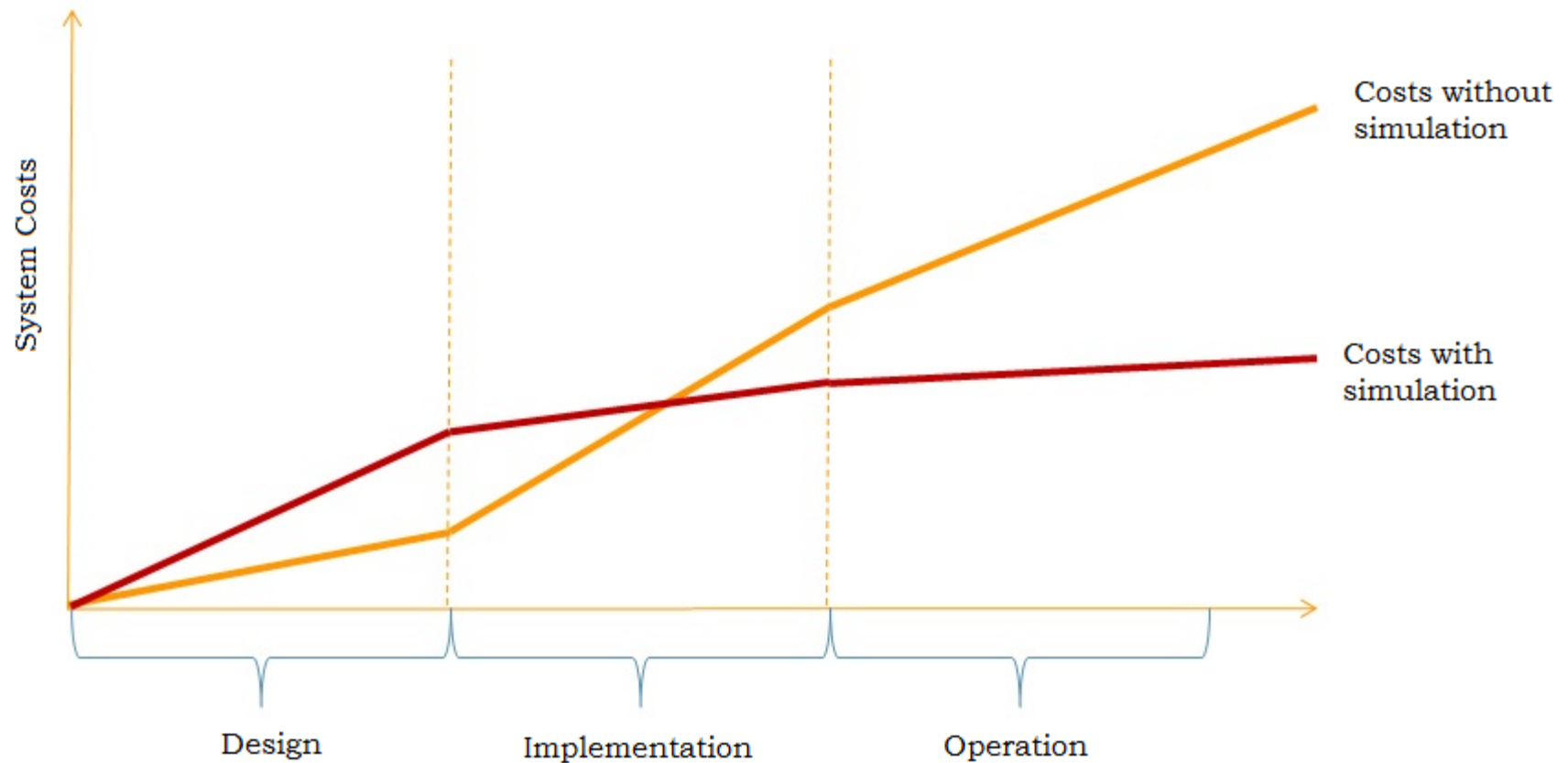
Simulation: limited scenarios set.

Optimization: Does not consider fluctuations in the model. Just in LP programs the sensitivity analysis.

- Advantages if they are together

Improvement in analysis aspects and consequent optimization when possible.

Simulation and Optimization

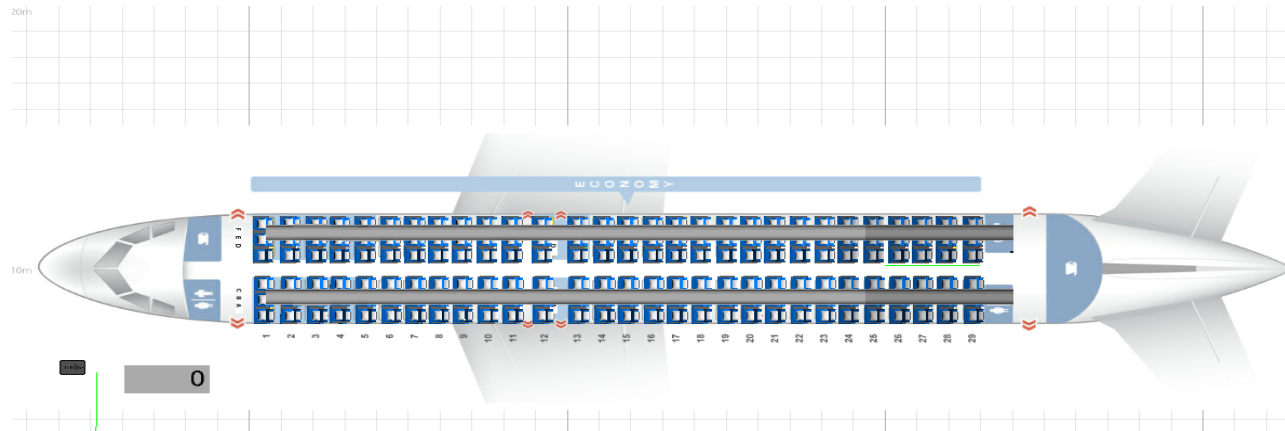


Case 1 Boarding process

The boarding process of an aircraft is part of the critical path in the turnaround process of an aircraft. This case presents a binary integer programming model to solve the problem, testing different configurations with simulation.

Boarding process

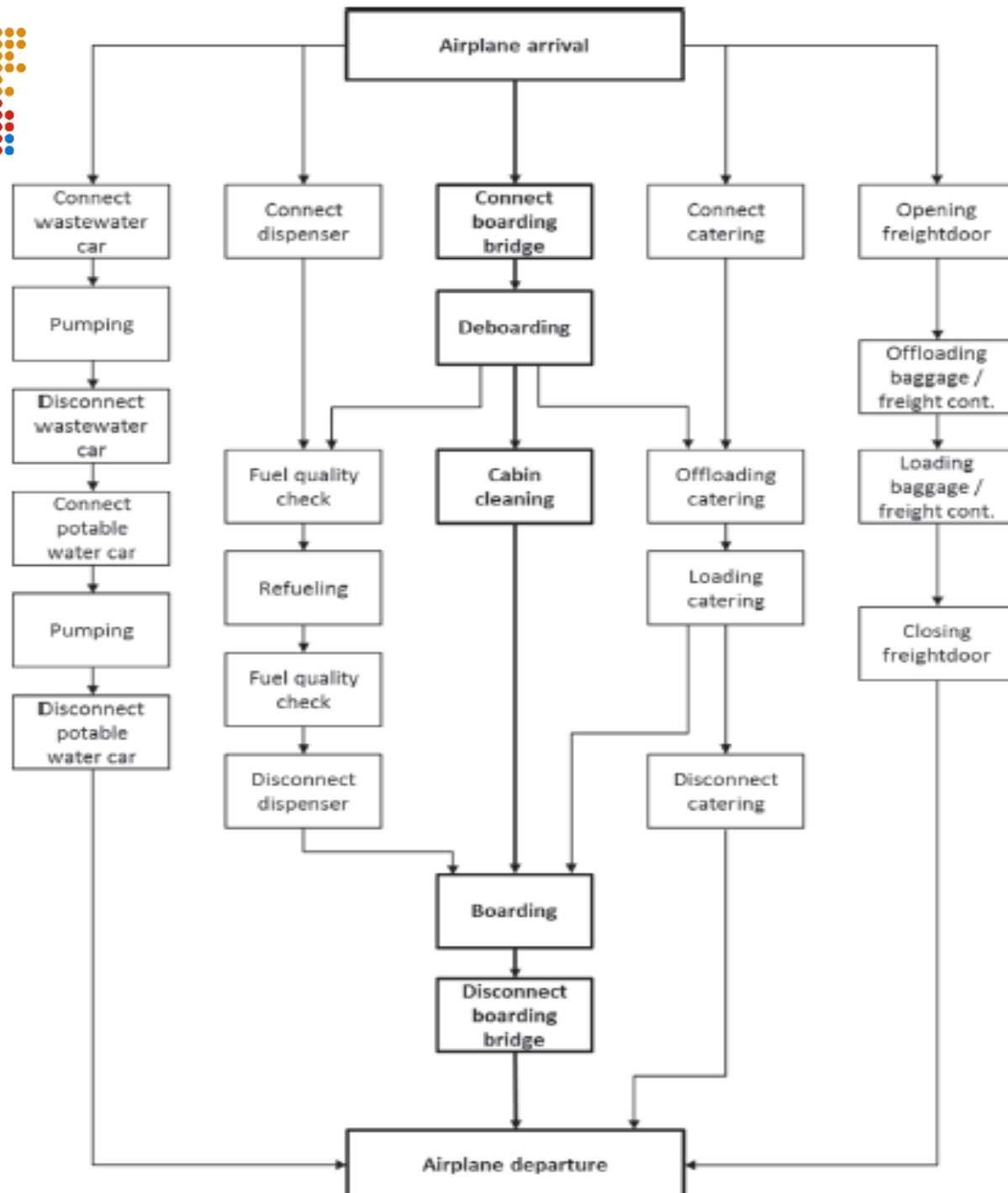
The turnaround time (TAT) of an aircraft is the temporary space between consecutive flights when the aircraft is in the airport.



Different times according with business

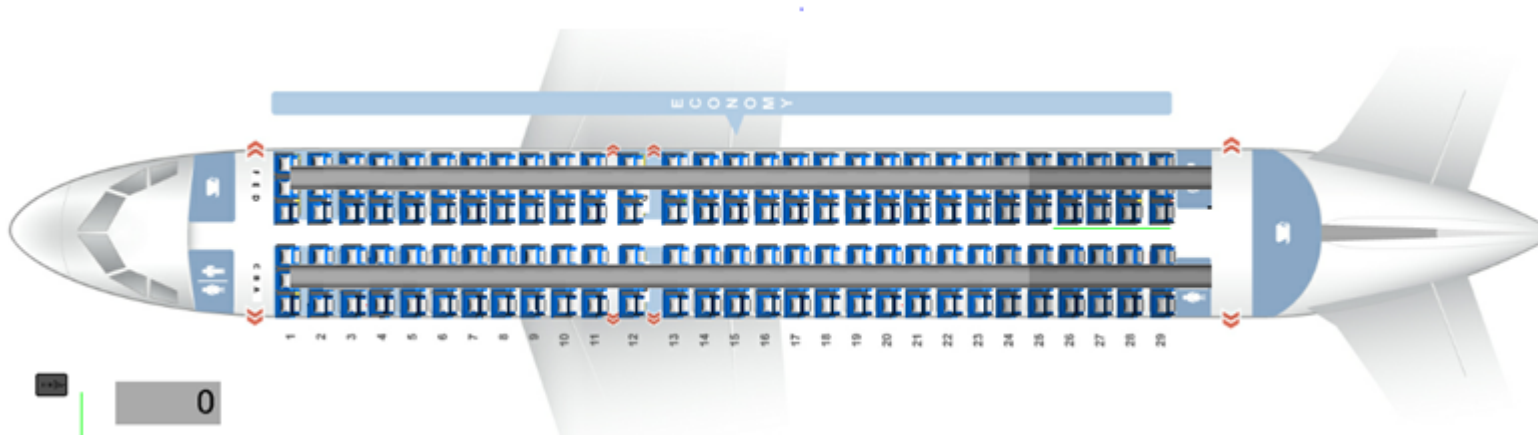
TAT of a Low Cost Carrier (LCC) is much smaller than the one for the Full Service Carrier (FSC).

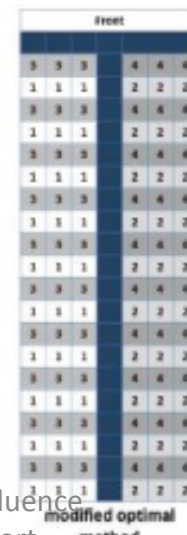
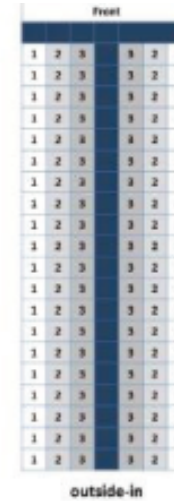




Reducing TAT

In order to reduce the TAT it is necessary to reduce as much as possible the time of the steps that compose the critical path.





Boarding strategies used

Strategy	Description	Advantages	Drawbacks	Usage
Random	Just one boarding group; there is no given sequence for the passengers to board, but every passenger is assigned to a particular seat	No organizational effort with calling groups; easy to understand; passengers who are traveling in a group can board together; rather fast; late passengers do not influence efficiency	Very bad worst case performance	Common (e.g., American Airlines, Lufthansa)
By group				
Back-to-front	Boarding in blocks from the back of the plane to the front	Easy to realize; passengers who are traveling in a group can board together	Congestions are concentrated on a small area of the plane; rather slow	Common (e.g., Delta Air Lines, US Airways, Lufthansa)
Outside-in/WiIMA	First all window seats, then middle seats, finally aisle seats	Fast because of no seat interferences	Separation of passengers who are traveling in a group	Rare (e.g., United Airlines)
Reverse-pyramid	Mixture of <i>back-to-front</i> and <i>outside-in</i>	Fast	Rather complicated; separation of passengers who are traveling in a group possible	Rare
By block	Passengers of some consecutive rows board together; generalization of <i>back-to-front</i> ; also possible <i>front-to-back</i> ; possible to skip rows/blocks and board them later	Passengers who are traveling in a group can board together	Congestions are concentrated on small areas of the plane; slow if more than one block (= <i>random</i>), the more blocks, the slower	Other variants than <i>back-to-front</i> are rare
By half-block	Passengers of some consecutive rows and one side of the aisle board together	Passengers who are traveling in a group can board together	Rather slow	No usage known
By row	Passengers of one row board together	Passengers who are traveling in a group can board together	Slow; many boarding groups	No usage known
By half-row	Passengers of one row and one side of the aisle board together	Fast if rows are skipped; passengers who are traveling in a group can board together	Rather complicated	No usage known
By seat	Passengers board individually in given optimal order; number of boarding groups = number of passengers	Optimal sequence → fastest possibility	Complicated; difficult to realize/to explain to passengers; separation of passengers who are traveling in a group	Rare (e.g., Southwest Airlines)
Steffen method	Exactly two rows distance between adjacent passengers (23A, 21A, 19A, ...)	Very fast because of no seat and just few aisle interferences (maximum number of passengers can stow baggage simultaneously)	Separation of passengers who are traveling in a group; rather complicated	No usage known
Open seating	There are no assigned seats; passengers can choose any free seat when entering the plane	No organizational effort with calling groups; traveling groups can board together; passengers can avoid interferences by thoroughly choosing their seats	Often perceived as stressful by the passengers; disadvantages of first-come, first served principle; last passengers who are traveling in groups probably do not get adjacent seats	Relatively common at low-cost carriers (e.g., Southwest Airlines, Ryanair)

Methodology

The current methodology presents an integer programming (IP) model that allows to integrate the characteristics that play a role in the boarding process and also to check different configurations with the IP model using simulation, since the IP model does not have a sensitivity analysis available.

IP Model

$$\begin{aligned}
 \text{Minimize } Z = & t_a \sum_{i=1}^N \sum_{j=1}^6 \sum_{k=2}^G AB_{ijk} + t_a \sum_{i=1}^N \sum_{j=1}^6 \sum_{k=1}^G AW_{ijk} \\
 & + t_s \sum_{i=1}^N \sum_{k=2}^G (SB_{i1k} + SB_{i2k} + SB_{i5k} + SB_{i6k}) \\
 & + t_s \sum_{i=1}^N \sum_{k=1}^G (SW_{i1k} + SW_{i2k} + SW_{i5k} + SW_{i6k}) \quad (1)
 \end{aligned}$$

In the above formulation, Eq. (1) indicates that the objective is to minimize the time required to eliminate the total number of interferences among all passengers, which is equal to the sum of between-group aisle interferences, within-group aisle interferences, between-group seat interferences, and within-group seat interferences.

Constraints

Definitional constraints

$$\text{subject to: } AB_{ijk} \geq -M(1 - x_{ijk}) + \alpha \left[\sum_{u=1}^i \sum_{v=1}^6 x_{uvk} - 1 \right],$$

$$i = 1, 2, \dots, N; j = 1, 2, \dots, 6; k = 2, 3, \dots, G \quad (2)$$

$$AW_{ijk} \geq -M(1 - x_{ijk}) + 0.5 \left[\sum_{u=1}^i \sum_{v=1}^6 x_{uvk} - 1 \right], \quad i = 1, 2, \dots, N;$$

$$j = 1, 2, \dots, 6; k = 1, 2, \dots, G \quad (3)$$

$$SB_{i1k} \geq -M(1 - x_{i1k}) + \sum_{w=1}^{k-1} x_{i2w} + \sum_{w=1}^{k-1} x_{i3w}, \quad i = 1, 2, \dots, N; k = 2, 3, \dots, G \quad (4)$$

$$SB_{i2k} \geq -M(1 - x_{i2k}) + \sum_{w=1}^{k-1} x_{i3w}, \quad i = 1, 2, \dots, N; k = 2, 3, \dots, G \quad (5)$$

$$SB_{i3k} \geq -M(1 - x_{i3k}) + \sum_{w=1}^{k-1} x_{i4w}, \quad i = 1, 2, \dots, N; k = 2, 3, \dots, G \quad (6)$$

$$SB_{i6k} \geq -M(1 - x_{i6k}) + \sum_{w=1}^{k-1} x_{i4w} + \sum_{w=1}^{k-1} x_{i5w}, \quad i = 1, 2, \dots, N; k = 2, 3, \dots, G \quad (7)$$

$$SW_{i1k} \geq 0.5[-M(1 - x_{i1k}) + x_{i2k} + x_{i3k}], \quad i = 1, 2, \dots, N; k = 1, 2, \dots, G \quad (8)$$

$$SW_{i2k} \geq 0.5[-M(1 - x_{i2k}) + x_{i3k}], \quad i = 1, 2, \dots, N; k = 1, 2, \dots, G \quad (9)$$

$$SW_{i5k} \geq 0.5[-M(1 - x_{i5k}) + x_{i4k}], \quad i = 1, 2, \dots, N; k = 1, 2, \dots, G \quad (10)$$

$$SW_{i6k} \geq 0.5[-M(1 - x_{i6k}) + x_{i4k} + x_{i5k}], \quad i = 1, 2, \dots, N; k = 1, 2, \dots, G \quad (11)$$

Constraints 2

$$\sum_{k=1}^G x_{ijk} \leq 1, \quad i = 1, 2, \dots, N; j = 1, 2, \dots, 6 \quad (12)$$

$$\sum_{i=1}^N \sum_{j=1}^6 x_{ijk} \geq L, \quad k = 1, 2, \dots, G \quad (13)$$

$$\sum_{i=1}^N \sum_{j=1}^6 x_{ijk} \leq U, \quad k = 1, 2, \dots, G \quad (14)$$

$$\sum_{i=1}^N \sum_{j=1}^6 \sum_{k=1}^G x_{ijk} = \lfloor \beta(6N) \rfloor \quad (15)$$

$$x_{ijk} = 0 \text{ or } 1, \quad i = 1, 2, \dots, N; j = 1, 2, \dots, 6; k = 1, 2, \dots, G \quad (16)$$

The purpose of Eq. (12) is to ensure that each passenger will be assigned to no more than one boarding group, Eqs. (13) and (14) are imposed so that the size of each boarding group will fall within the desirable range, and Eq. (15) states that the total number of seats taken is equal to the total number of passengers to board the plane. Lastly, Eq. (16) indicates that all decision variables are binary.

Simulation results

Results for an A320 economy section 138 passengers

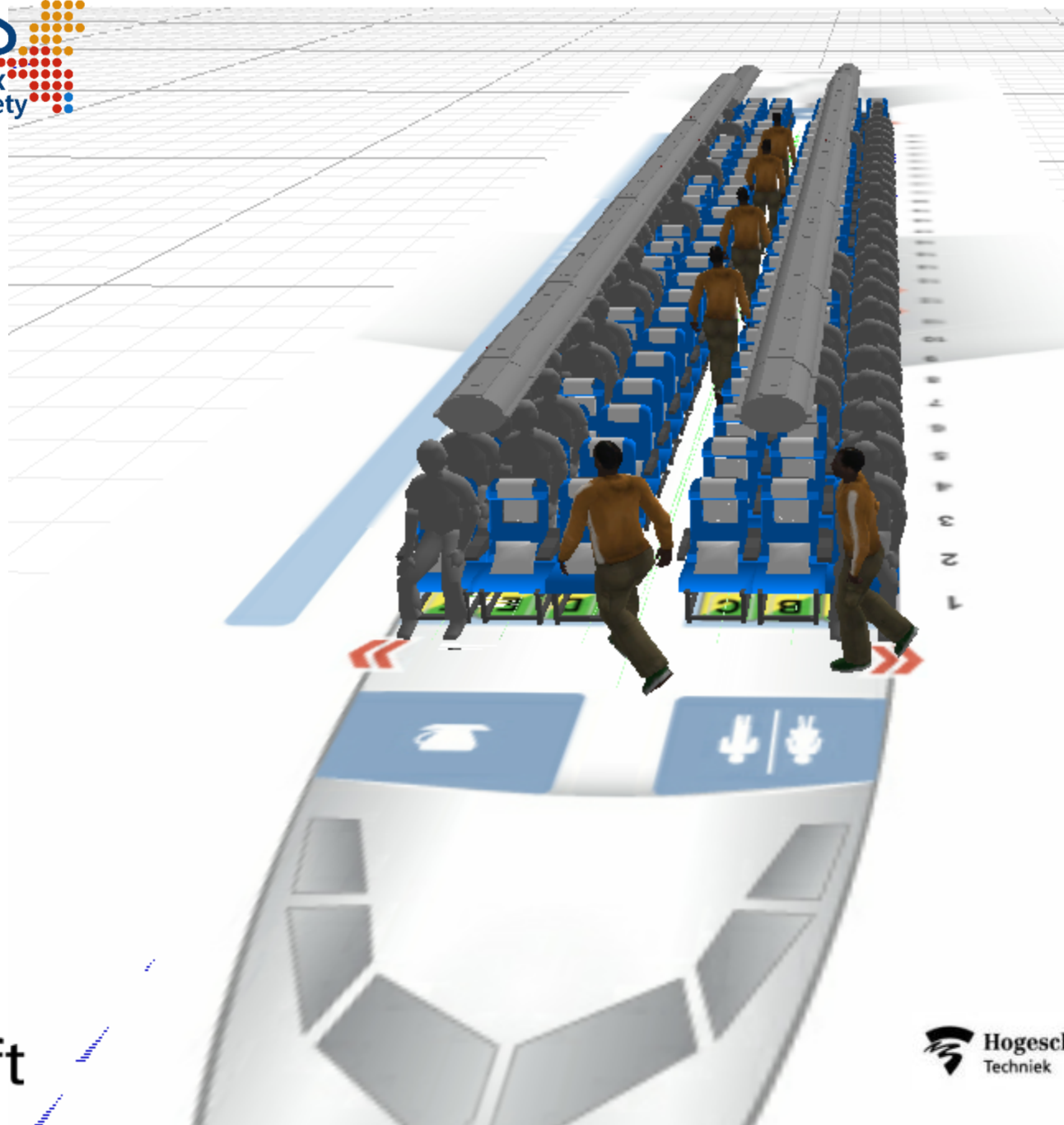
Speed 0.8 m/s	AVG	MIN	MAX	HALF WIDTH
Rear to Front OUT_IN	9.2928	9.0434	9.5242	0.0317
Rotating Zone OUT-IN	9.3495	9.1	9.5809	0.0317
Block Boarding (Ordered)	9.2928	9.0434	9.5242	0.0317
Block Boarding (Random)	9.753	9.5165	9.9892	0.0309
WiLMA (Outside-in)	9.2928	9.0434	9.5242	0.0317
Reverse Pyramid	9.2928	9.0434	9.5242	0.0317
Random assigned	9.9674	9.7319	10.2313	0.0318
Steffen	9.2798	9.0303	9.5112	0.0317
Random selected 1	9.4661	9.2167	9.6976	0.0317
random selected 2	9.3387	9.0893	9.5702	0.0317
random selected 3	9.3786	9.1227	9.621	0.0321

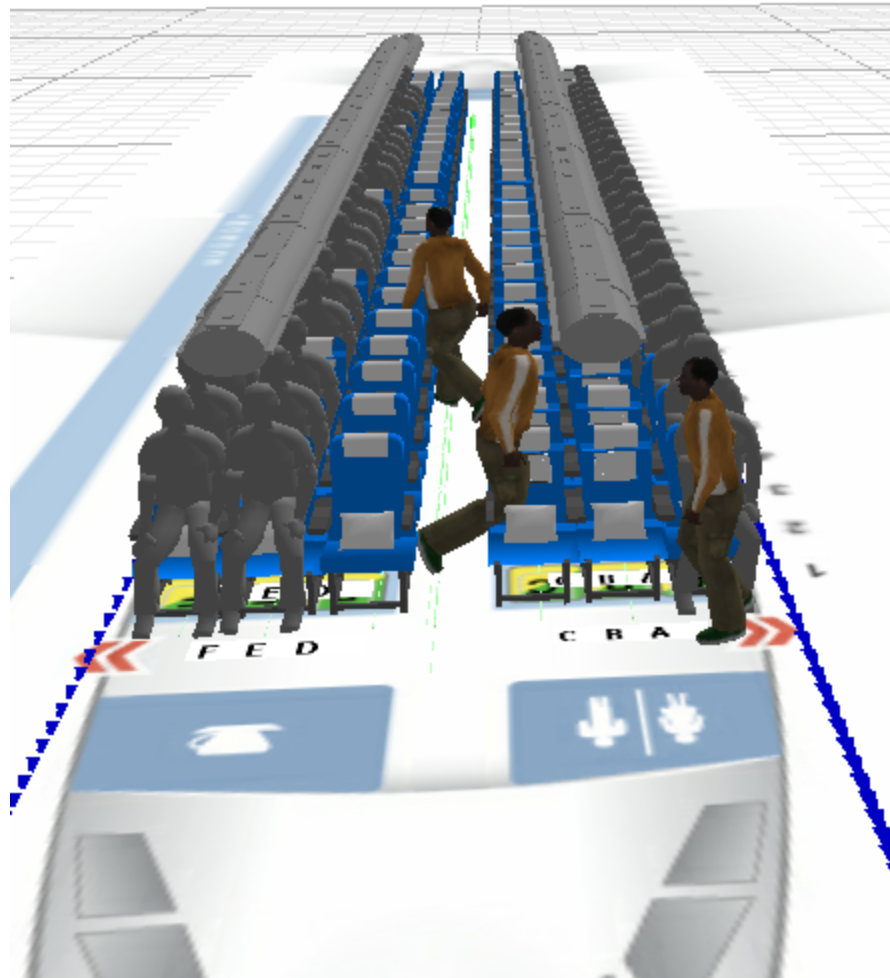
Ranking based on max

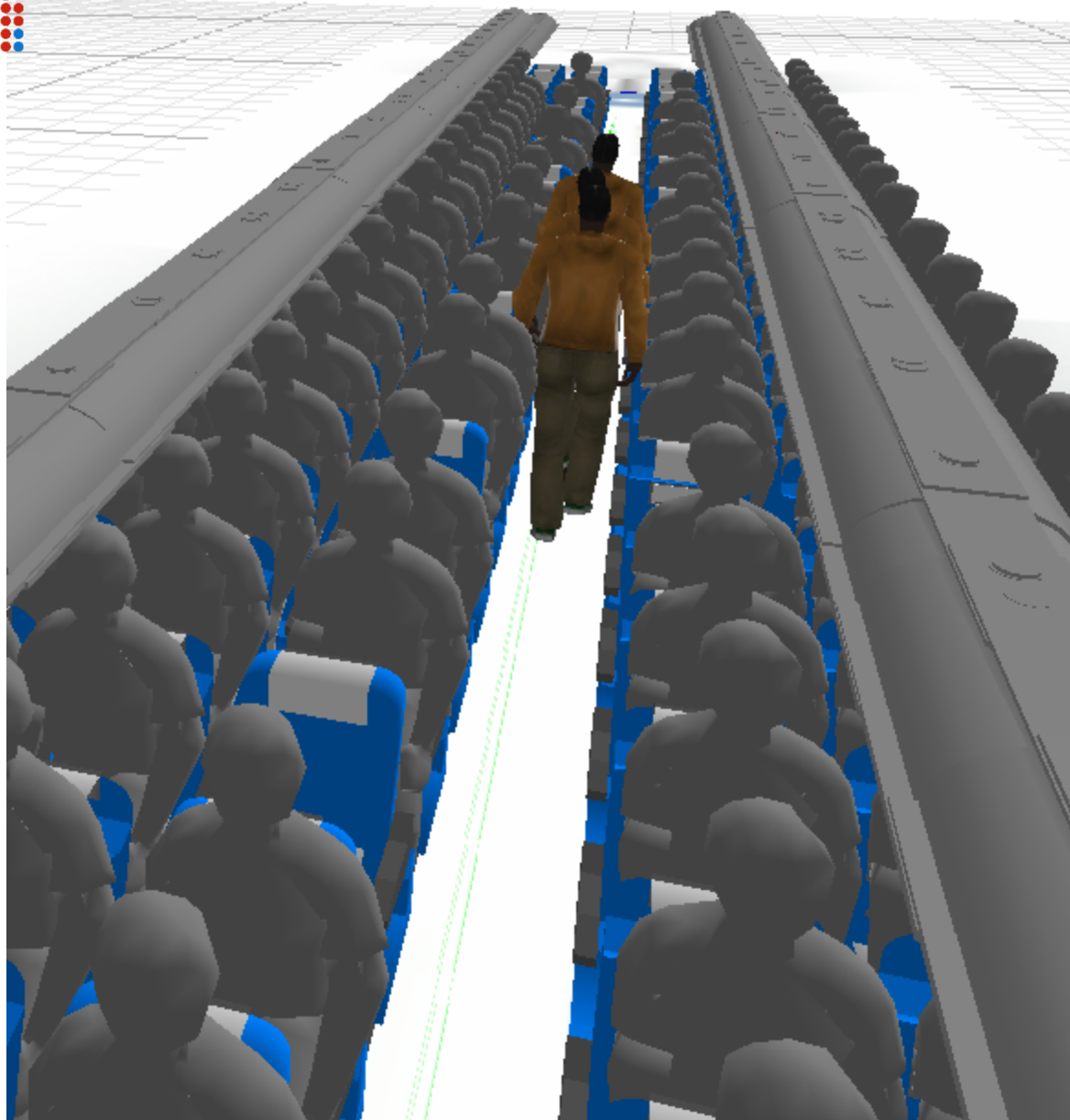
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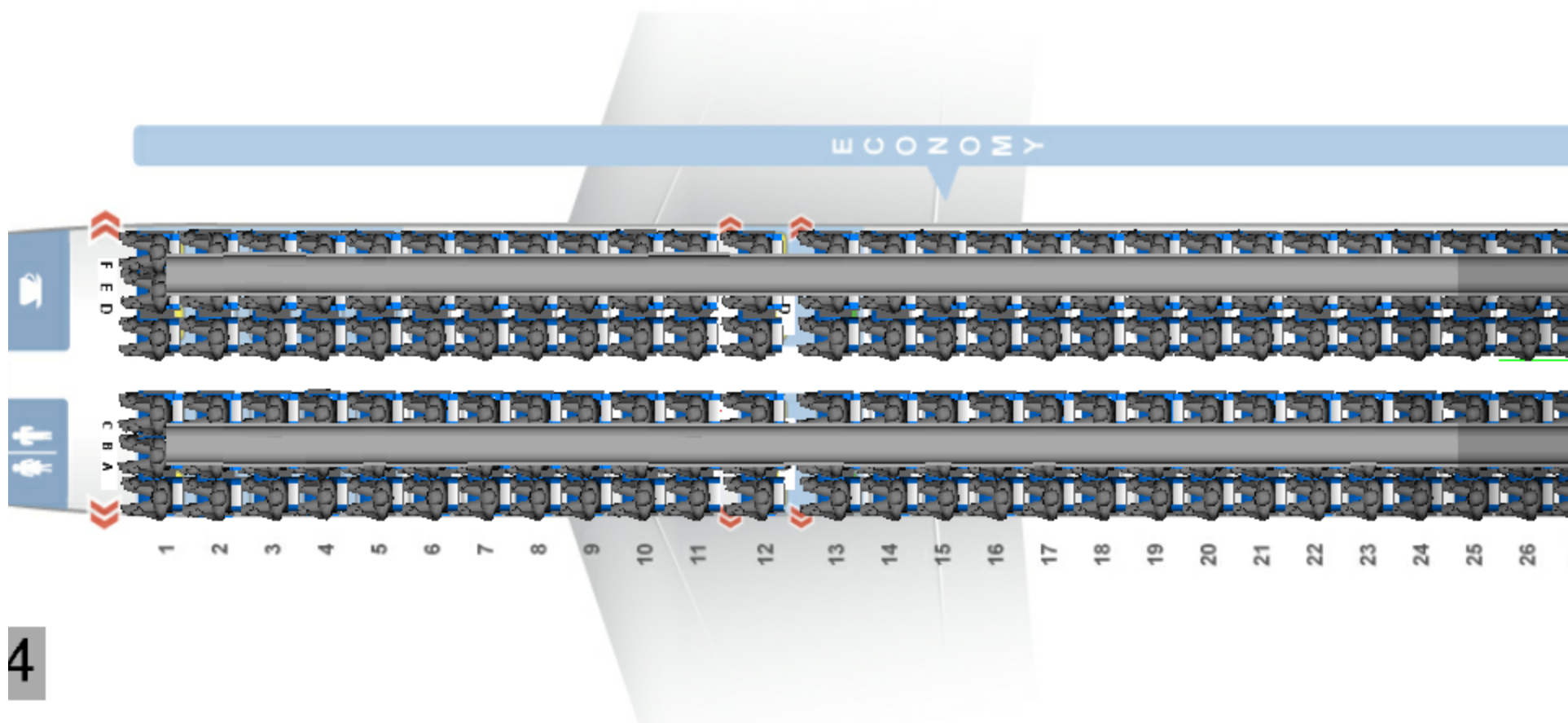
Ranking based on min

Speed 0.8 m/s	AVG	MIN	MAX	HALF WIDTH
Steffen	9.2798	9.0303	9.5112	0.0317
Rear to Front OUT_IN	9.2928	9.0434	9.5242	0.0317
Block Boarding (Ordered)	9.2928	9.0434	9.5242	0.0317
WiLMA (Outside-in)	9.2928	9.0434	9.5242	0.0317
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Conclusions

Based on this research we found a good boarding scheme but more experiments are needed, for different aircraft models and to compare the IP program with other mathematical models.

Case 2 Mexico city mobility

- The activities of managing and planning services in a context of cities entails a lot of work and participation of experts in different areas.
- Such is the case of transport that currently represents a challenge for researchers from different areas.
- There are three measures used for transportation analysis: traffic, mobility and accessibility.

Introduction

- Mexico City is divided by sectors; each sector has its own local responsibilities of management.
- A research about certain aspects of Mexico City should be conducted at different levels.
 - ✓ Considering the complete city, at macro level.
 - ✓ Second level the relationship between the different political sectors.
 - ✓ Third level analyze each sector individually.

Map of Mexico City with sectors



Traffic congestion

- Last year Mexico City ranked the highest congestion level on the road network, causing more than 90% extra travel time for citizens during busy hours.
- The aim of this study is to carry out a diagnosis about the public transport network in Mexico City for proposing a pertinent theoretical tool to optimize its operations on a daily basis.

Socio-economics KPI's of Mexico City

Periods of high growth without effective planning and increasing motorization, have pushed Mexican cities towards a “3D” urban growth model: distant, disperse, and disconnected.

The 3D model is a direct result of national policies subsidizing housing projects in the outskirts of urban agglomerations, managing urban and rural land poorly, and prioritizing car-oriented solutions for transportation.

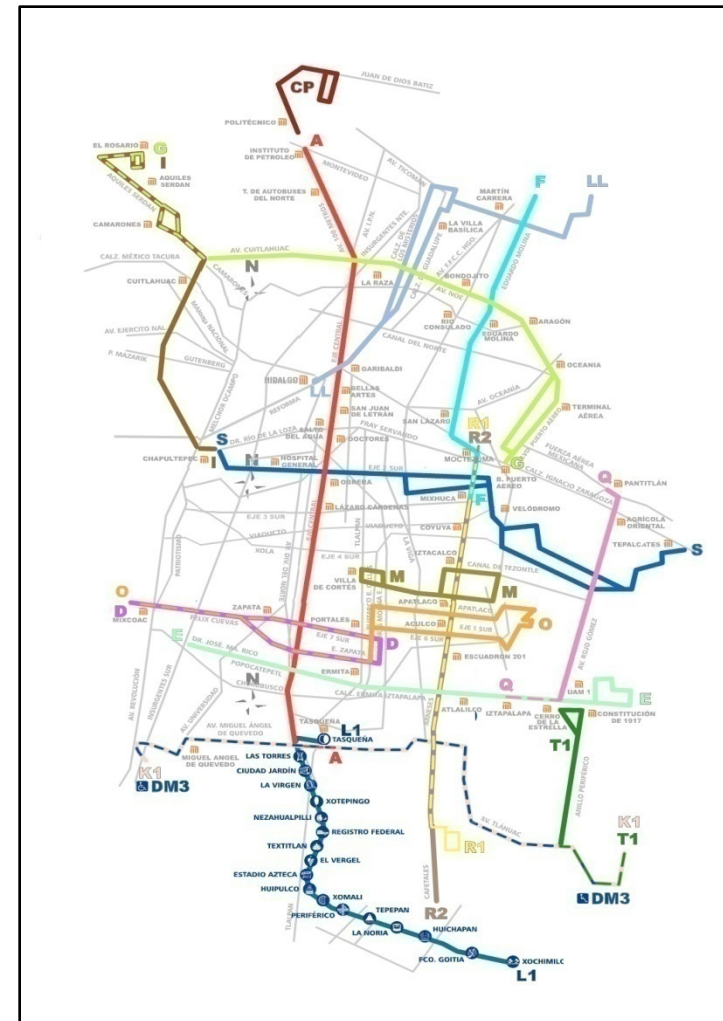
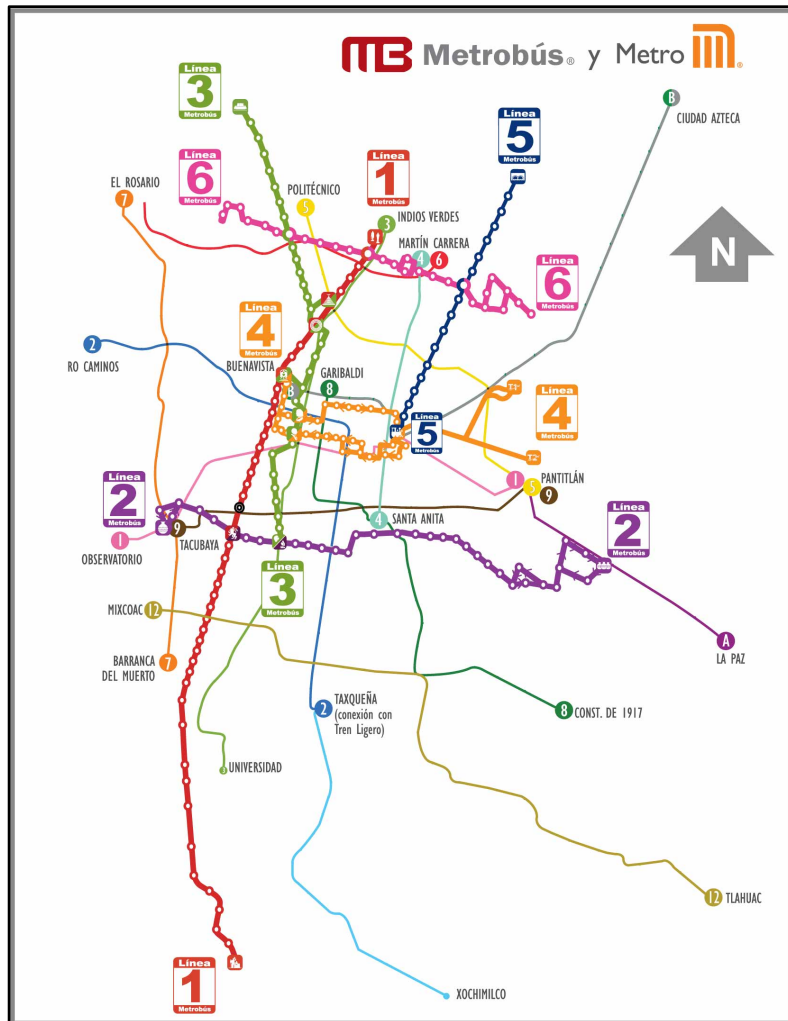
The alternative is a 3C urban growth model: Compact, connected and coordinated.

Administrative organization	The metropolitan area of Mexico is composed of 16 Delegations in the Federal District, 58 municipalities in State of Mexico, and 1 Municipality in State of Hidalgo.
Population (2008)	Federal District: 8.8 million Metropolitan area (Federal District and State of Mexico): 19.2 million
Area (2010)	Federal District: 1,487 km ² Metropolitan area: 7,180 km ² (40.1% of which is urbanized)
Population density (2010)	Federal District: 5,958 people/km ² Metropolitan area: 6,671 people/km ²
Annual population growth rate (2005 - 2010)	Federal District: 1.49% Metropolitan area: 3.96%
GDP and growth (2011)	163.6 billion USD (17% of the national GDP, Federal District only) Annual GDP growth (2008-2011): 4%
Unemployment rate (2011)	6.5%

Mobility in Mexico City

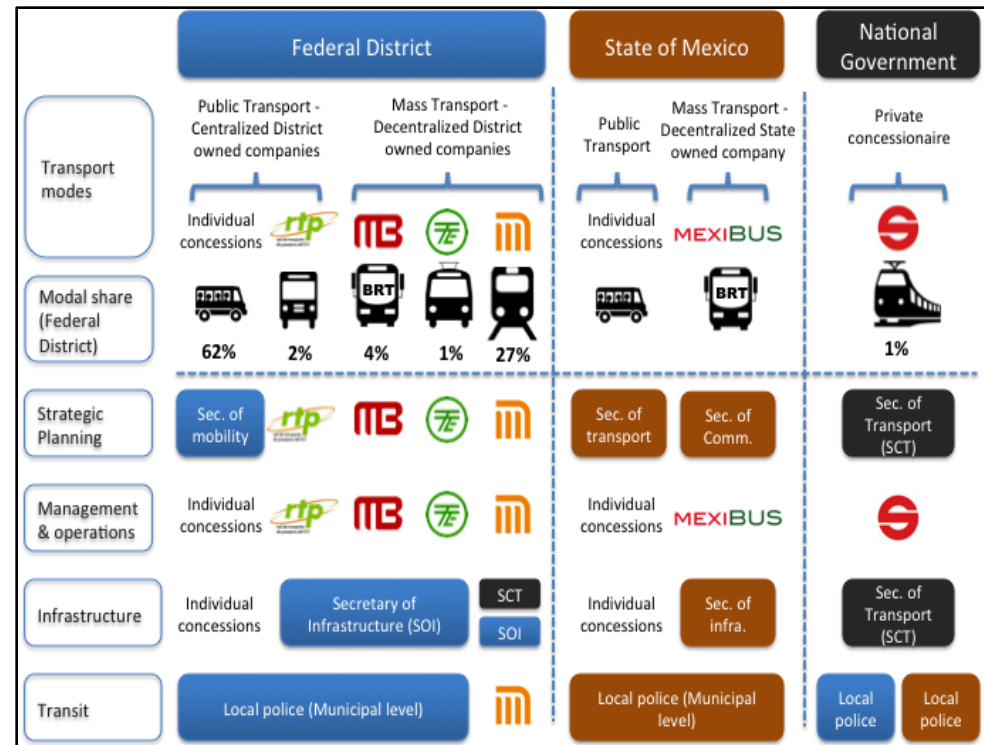
Total trips per day (2007)	48.8 million (Metropolitan area) and 32.0 million (Federal District)						
Daily trips per person (2007)	2.5 (Metropolitan area) and 3.6 (Federal District)						
Trips and modal share in the Federal District (2007)	Mode		Trips		% Total	% Public transport	
	Non motorized		8,600,000		26.9%		
	Private vehicles		4,800,000		15.0%		
	Microbuses		9,448,800		29.5%	50.8%	
	Metro		4,984,800		15.6%	26.8%	
	Autobuses		1,878,600		5.9%	10.1%	
	Taxis		1,041,600		3.3%	5.6%	
	Metrobus		762,600		2.4%	4.1%	
	Trolley (RTP)		204,600		0.6%	1.1%	
	Suburban train		167,400		0.5%	0.9%	
	Light train		111,600		0.3%	0.6%	
	Total		32,000,000		100.0%	58.1%	
Road network (2007)	10,200 km (91% local roads)						
Total vehicles (Federal District, 2001)	Cars				4,460,386		
	Taxis				225,302		
	Motorcycle				11,920		
	Microbuses				20,459		
	Buses				8,240		
	Combis				3,519		
	Metrobus – articulated buses				322		
	Metrobus – regular buses				54		
	Metrobus – biarticulated buses				27		
	Totals				4,730,228		
Road safety (2010)	Total number of accidents				14,729		
	Number of deaths				1,026		
	Involved vehicle in deaths				81.0% Car 5.6% Truck 3.5% Microbus		
	Involved victim in deaths				52.0% Pedestrian 20.0% Car driver 14.0% Motorcycle driver		
Emissions (contribution by vehicle type) (2006)	Pollutant	Cars	Taxis	Microbuses	Buses	Motorcycles	Trucks
	CO ₂	58.0%	6.2%	13.2%	1.9%	6.0%	14.7%
	NO _x	46.2%	6.9%	11.4%	10.2%	1.0%	24.3%
	PM _{2.5}	14.2%	2.4%	1.6%	25.2%	1.5%	55.1%

The public transport network in Mexico City context



Management of Public Transport

- The management of the public transport in Mexico City is fragmented and this makes it difficult to establish some planning policies for its improvement



Complex networks

The public transport networks in Mexico City are considered complex and both vulnerability and resilience are important factors to take into account. As Reggiani (2015) states, the following questions need to be answered:

- Is a complex network a necessary condition for the emergence or presence of transport resilience and vulnerability?

“the term ‘complexity’ embeds both the assemblage of different units in a system and their intertwined dynamics.

Furthermore, connectivity is one of the essential elements that characterize complex networks.



Complex Networks

- Several indicators of resilience and vulnerability co-exist; are these differences related to specific fields of transportation research?

Resilience and vulnerability conditions associated with such hubs can then impact on the resilience/ vulnerability of the whole network.



Complex Networks

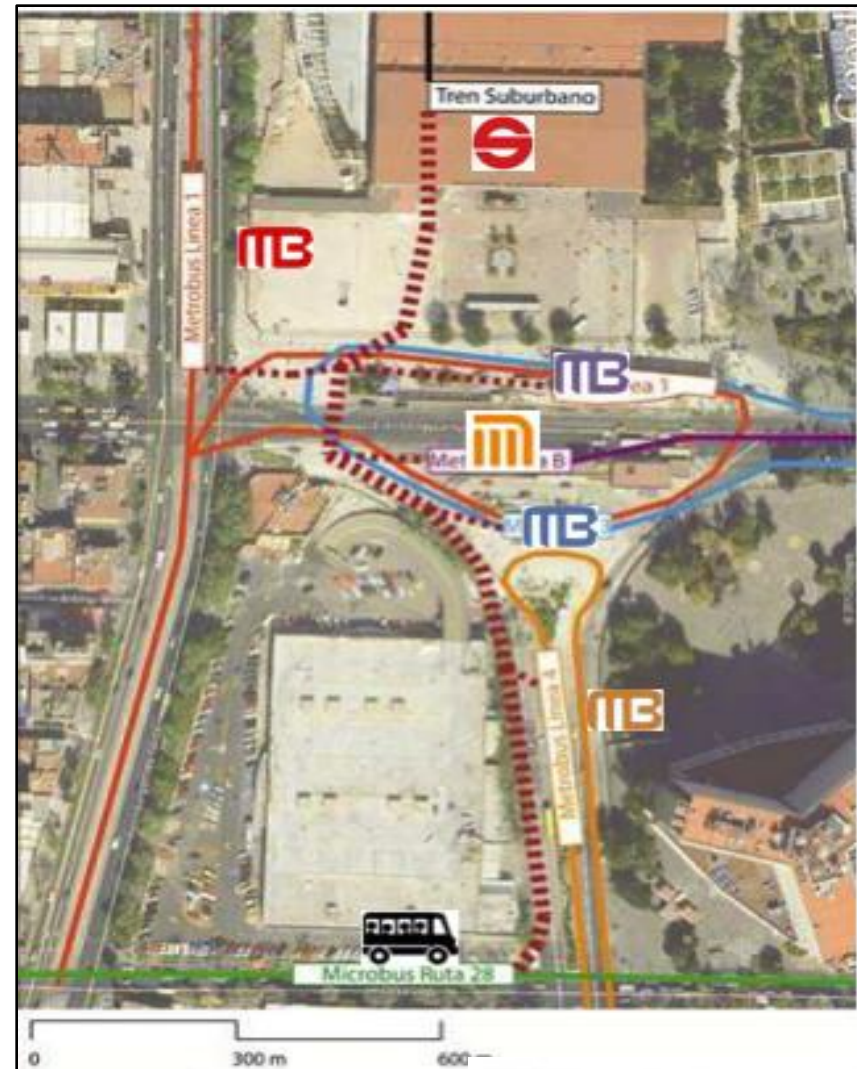


Can connectivity or accessibility be considered as a unifying framework for understanding and interpreting – in the transport literature – the concepts of resilience and vulnerability?

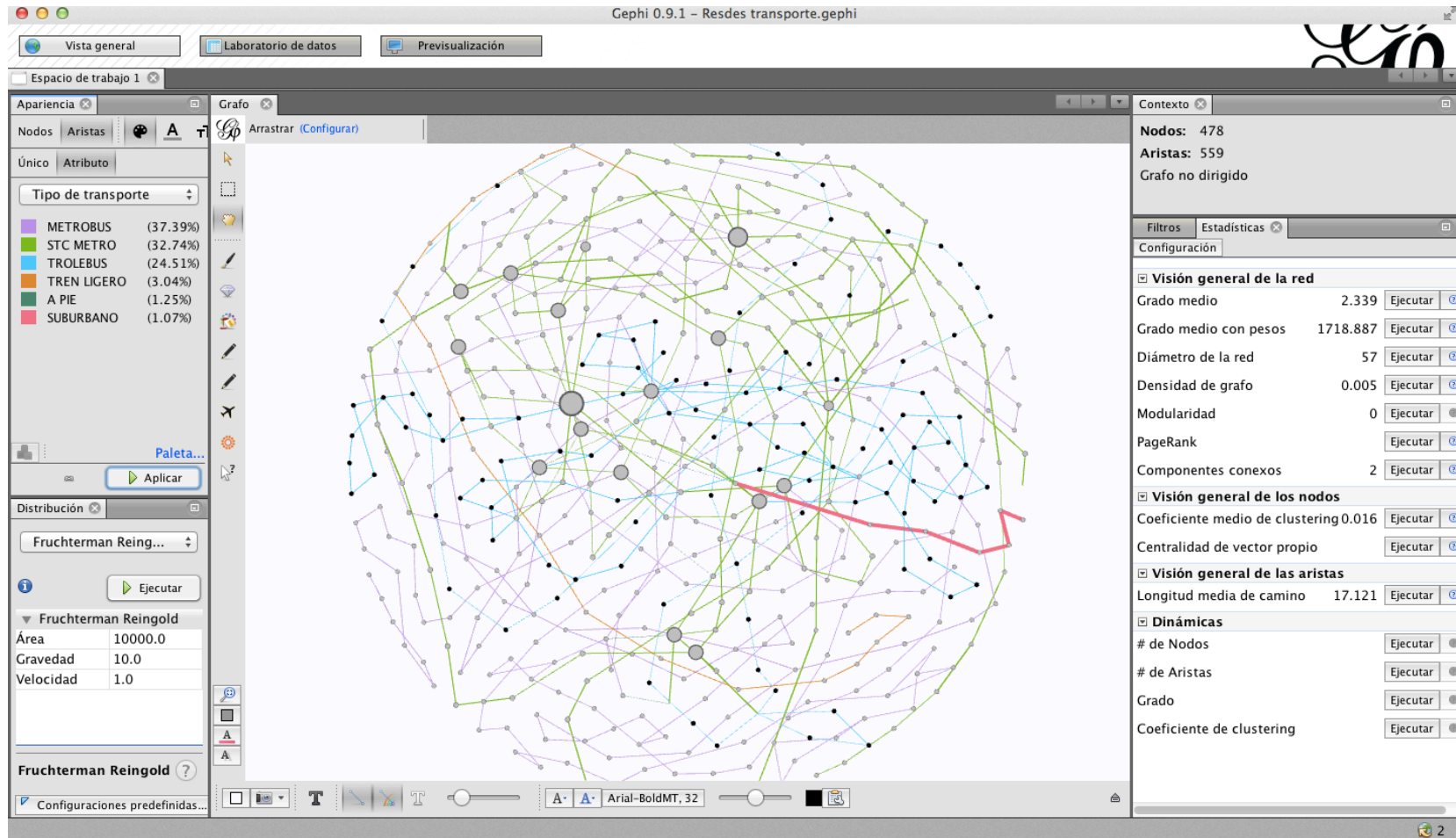
For optimizing urban mobility in Mexico City, we propose to carry out a network analysis based on traffic, mobility and accessibility aspects to develop a simulation model.

An example of disconnected network

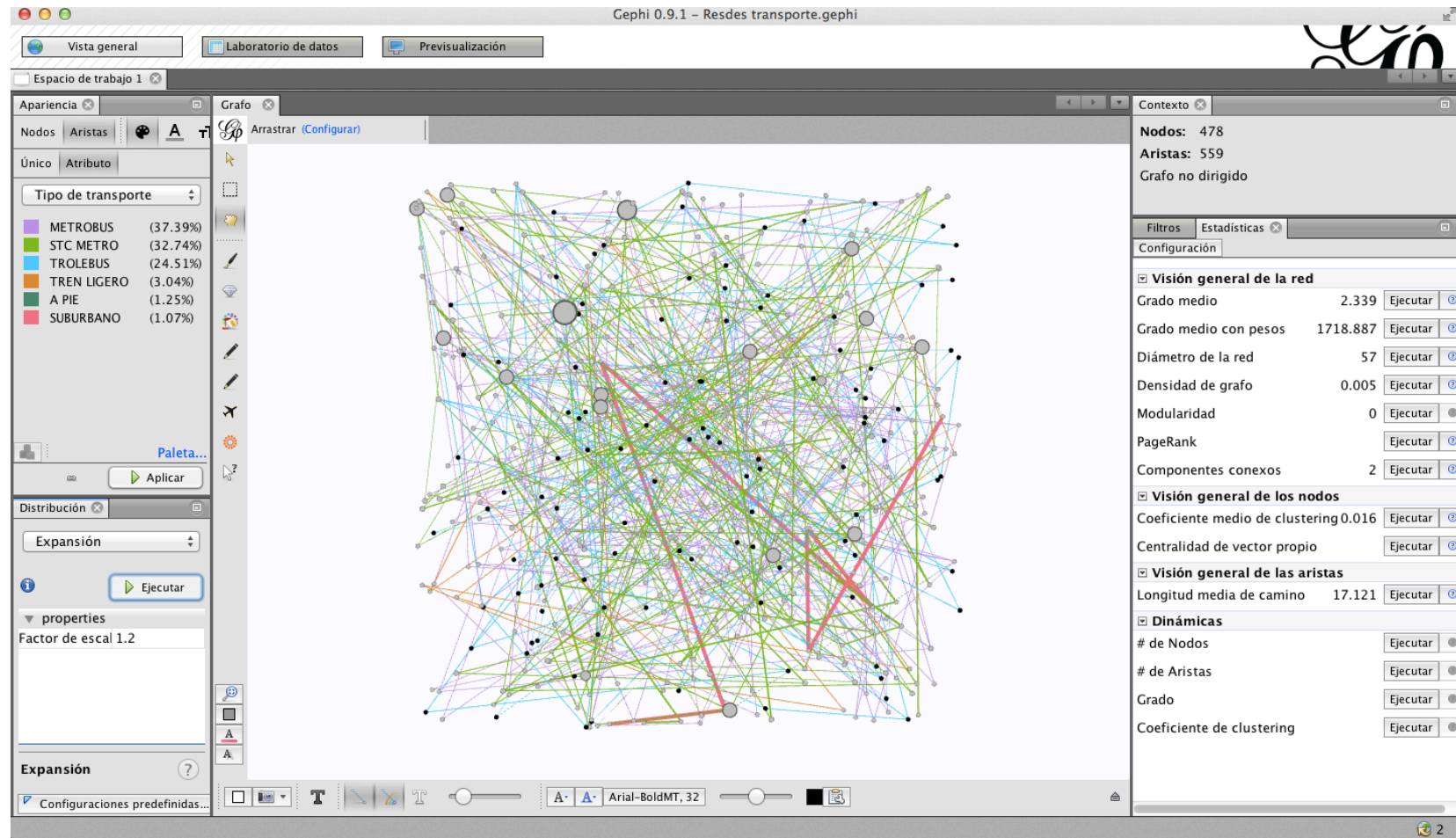
In Buenavista - an area of Mexico City where three modes of transport converge – travellers must walk up to 1.5 km to transfer from one mode to another. Close to 150,000 users use this disconnected transport hub every day with significant costs for users as well as for operators.



Suburban train

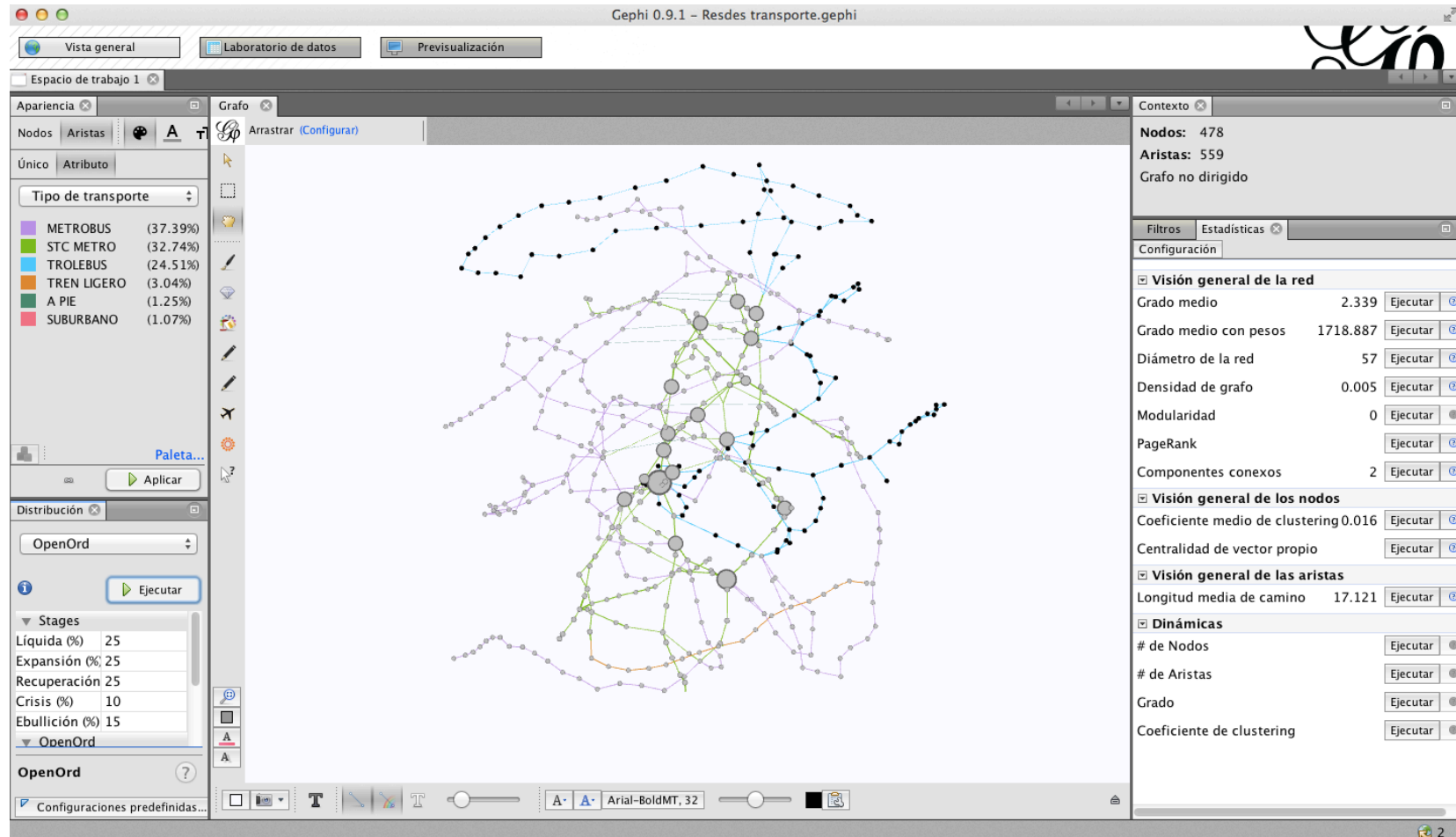


Different modes



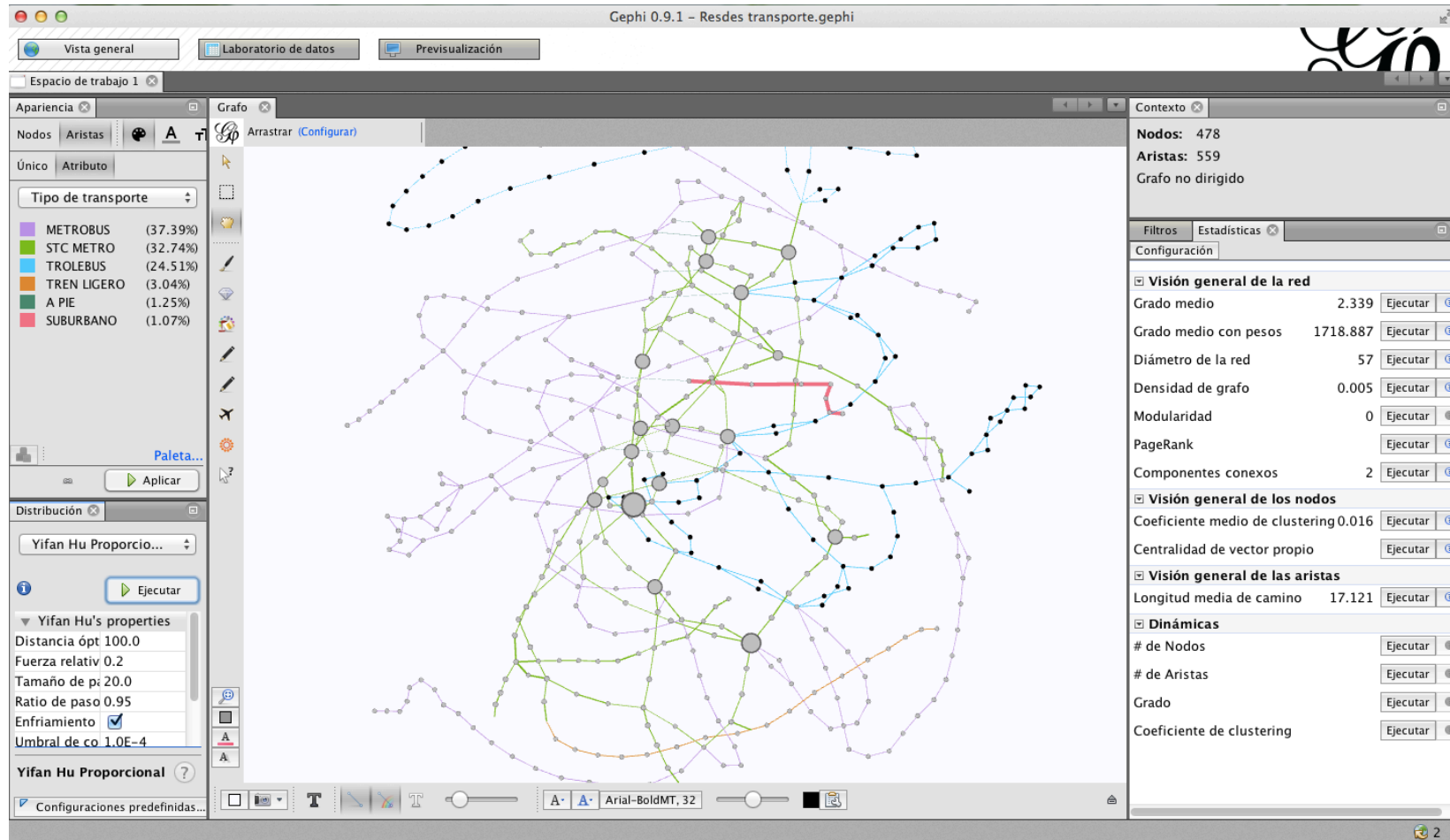
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Centroids



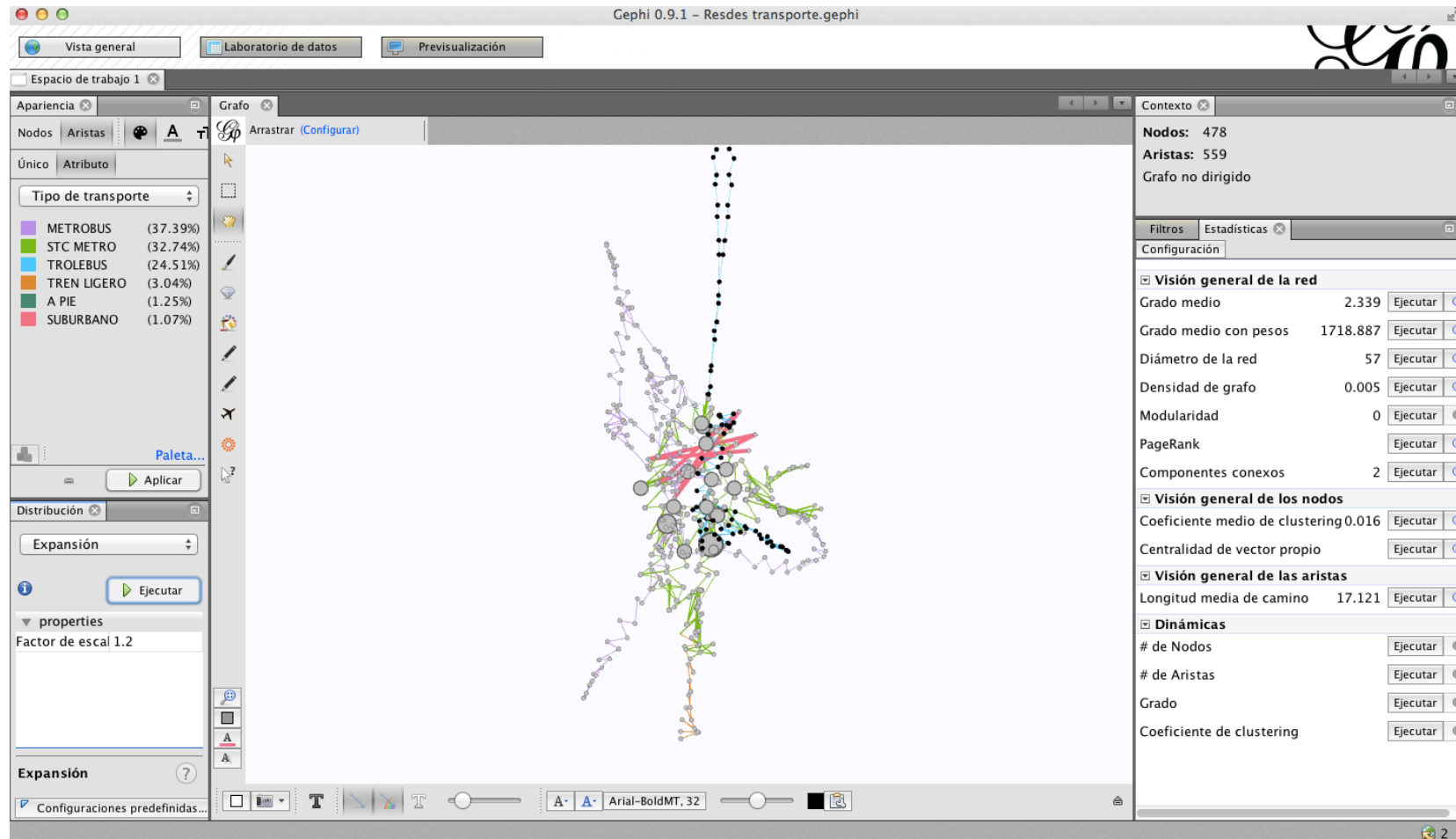
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Disconnected nodes



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General view



Conclusions

- Recent studies that have been made on mobility in Mexico City have a transportation management approach, but they have not used a systemic approach and made use of quantitative tools such as simulation and optimization.
- As we can see the analysis proposed is innovative because it considers the transport network as a complex network that has as an important issue with the disconnection.
- At a macro level, connectivity analysis is verified through an optimization algorithm, then the simulation is used to design simulation scenarios and search for feasible solutions.
- For future research some results in the macro level will be available, a mezzo and micro level analysis will be developed.

THANK YOUU!!

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